

Flipping a coin between states in Ch. I.

2	1	0	1
14	2	2.5	2.5
3	2	2.5	2.5
2	1	0	1

P_x^H C_x P_x^T S_x

P_x^S S_x R_x^S T_x

$\frac{1}{2}P_x$ $\frac{1}{2}P_x$ $\frac{1}{2}P_x$ $\frac{1}{2}P_x$
 H_x E_x T_x S_x

7.5
13.5
37.5
18.75

150
37.5
17.5
27.5

$\frac{1}{2}x^2 - \frac{1}{2}x + \frac{1}{2}$

$$E(x) = \frac{1}{2}P \cdot 10 + \frac{1}{2}(1-P) \cdot 0 = \frac{1}{2}P \cdot 0 + \frac{1}{2}(1-P) \cdot 10$$

$$E(x) = \frac{1}{4}P \cdot 10 + \frac{3}{4}(1-P) \cdot 0 + \frac{3}{4}P \cdot 0 + \frac{3}{4}(1-P) \cdot 10$$

$$2.5P + 7.5(1-P) = 7.5 - 5P = 17.5 - 25P = 3.75$$

	H	T
R	R_H	R_T
P	0	10

The potential distribution of outcomes range from $(10, 0; \frac{1}{2}, \frac{1}{2})$ to $(10, 0; \frac{1}{2}, \frac{1}{2})$ as p_R ranges from 0 to 1.

so E is constant: 0

$$\frac{1}{2}p_R + \frac{1}{2}(1-p_R) = \frac{1}{2}$$

10	0
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Compute the possible distribution over the different outcomes.

$$\begin{array}{ccc}
 & 30 & 60 \\
 R & Y & S \\
 \hline
 10 & 0 & 10 \rightarrow & (10, 0; \frac{1}{3}, \frac{2}{3}, 0) \\
 0 & 10 & 10 \rightarrow & (10, 0; \frac{2}{3}, \frac{1}{3})
 \end{array}$$

Flipping coin between I and IV results in action whose expected payoff is midway between I + II; Ideal action has a single dist over outcomes, and so does any rest-combination.

But the dist. of outcomes to

$$\text{II is } (10, 0; \frac{2}{3}, 1 - \frac{1}{3})$$

$$\text{To III: } (10, 0; \underline{\frac{1}{3}} - 1, \frac{2}{3} - 0)$$

Dist over ~~the~~ outcomes for: $(\text{II}, \text{III}; \frac{1}{2}, \frac{1}{2})$ is $(10, 0; \frac{5}{12} - \frac{9}{12}, \frac{7}{12} - \frac{3}{12})$.

Thus, minimum prob. of 10 is higher than for either I or III (max prob. of 10 is lower). To extent that min is weighted more than max, combination will be preferred to either II or III.

	$\frac{1}{3}$	$\frac{2}{3}$	0	10	10	10	$(0, 0; \frac{1}{2}, \frac{1}{2})$
I	10	0	0	10	10	10	

	0	10	0	-10	0	10	$(0, 0; \frac{1}{2}, \frac{1}{2})$
II	0	10	0	-10	0	10	

I ~~and dominant~~ II, but \exists II

$$\frac{1}{2}P_1 + \frac{1}{2}P_2 = 0$$

$$\frac{1}{2}P_1(0) + \frac{1}{2}(0 - P_1)10$$

$$\begin{aligned} & \frac{3}{2} \\ & (0, 0; \frac{1}{2}, \frac{1}{2}) - \frac{1}{2} \cdot \frac{3}{2} \\ & (0 - \frac{3}{2}) \cdot 10 \end{aligned}$$

$$\begin{aligned} & \frac{1}{2} \\ & 10 \quad 0 \quad 0 \\ & 0 \quad 10 \quad 10 \quad \frac{1}{2} \cdot 10 + \frac{6}{12} \cdot 10 = \frac{7}{12} \cdot 10 \end{aligned}$$

$$\begin{aligned} & \frac{2}{3} \\ & (0, 0; \frac{2}{3}, \frac{1}{3}) - \frac{1}{3} \cdot \frac{2}{3} \\ & (0 - \frac{2}{3}) \cdot 10 \end{aligned}$$

$$\begin{aligned} & \frac{1}{4} \\ & 0 \quad 10 \quad 0 \quad 0 \quad \frac{1}{4} \cdot 10 + \frac{1}{6} \cdot 10 \rightarrow \frac{1}{2} \cdot 10 \end{aligned}$$

$$\begin{aligned} & \frac{3}{4} \\ & (0, 0; \frac{3}{4}, \frac{1}{4}) - (\frac{1}{3} - 1) \cdot 10 \end{aligned}$$

$$\begin{aligned} & \frac{3}{4} \\ & 10 \quad 0 \quad 10 \quad \frac{5}{12} \cdot 10 - \frac{9}{12} \cdot 10 \end{aligned}$$

The range of distribution over distinct outcomes is not the same for all actions; some have only one dist (risk)

But this that "expectation is known" or "forecasted" but - as
though uncertainty had been converted into risk certainty;
but that prob. dist. of outcomes is known; certain outcomes
are felt confidently to be "much more likely" than others, or
"equally likely"; in a large number of cases when you
attacked their likelihoods, when you had the case info and
confidence (e.g. in repetition of case but, if possible) you
would expect to win about half the time; and would so bet
on your compound winnings.

This is not true of "equal ignorance."
(imagine many wins of unknown contents).

This, a game, mixed mixed strategy often counts ignorance
into risk (if all effects from strat are included in his optimum
strat).

But note arguments about "best optimum" strat; why not give
up some on, wouldn't mind, to gain on others

Cont assign vN-M utilities to states with ambiguous
outcomes; if they are p-figs, they don't obey vN-M axioms.

When we are ignorant — don't feel sure as to relative
likelihoods — it ^{seems} to be influenced by the range of possible
outcomes more than by estimate of likelihood. This could amount
to "taking all outcomes into account equally"; equalizing prob.

But this rule would not tend to lead one away
from situations of ignorance when he had alternatives. You
don't want him to do this "blindly" — e.g. when worst outcome
cooperates favorably with best or expected outcome under
"risk" situation; or when "expected" outcome in ambiguous
situation is much better and worst isn't much worse.
Weighting worst states more, then, punishes choices against
ignorant gambles where expectation isn't much better and where
worst "reasonable case" is much worse than best guess.

My short report note:

Does random sample like random that, cannot measure
with much?

An action involving an observation may offer low once regret,
or constant & all regret (according to cost of delay + observation).
What else can be said about it?

Adaptiveness - robust + sparsification of memory.

Flexibility; segmented decision; postponement of choice;
liquidity; extensification; speed of reaction, communication, decision.

What do these have in common? What advantages; what
what conditions?

Do they lead to actions with similar payoffs, or regrets?

(Bsp: all but good under ignorance - not yet - if they don't cost
too much).

Speed of adjustment, etc., presumably related to likelihood of changes in environment
that are unpredictable long in advance; or, knowledge of whose long-run stochastic properties
is not enough for adequate adaptation. over

In some cases, knowledge of opponent's ^{long-run} mixed strategy might allow optimal or adequate long-run adjustment. Question is, value of short-run "intelligence" on his precise choice in an individual play, if combined with ability to adjust fast?

(Value of bomb alarm info; depends on ability to adjust, and on the potential value of adjustment).

Note that you don't automatically "know" what is happening, or what has happened, unless you take steps to acquire this info; especially in war.

Classmate

It can be too costly to build in delays for decision and adjustment response, when info is unlikely to arrive "in time" despite effort, and when value of adjustment is small (assumption of spam war proponents?).

I have war approach does reflect some practical wisdom, combined with bad assumptions; They tend to ask sensible questions; but they don't look for answers, and assume bad ones.

TWA

Sunday

\$100 9:00 AM 64 NY-4150
\$500 7:30 PM Paris 7:30 AM

Man who always chooses all the time and whose N.M. utility is concave will expect unfavorable payoffs lots; if these dominate many the lots offend him in the long run he will care more.
(At least one lot of the last was predicted.)

Long-run arguments really favor managing expectation of money (with more of expected convex utility being somewhat non-conservative; man you will take lots only at good enough odds, from long-run expectation will be lower but the prob. of ruin is also lower).

On Committee problem:

Disagreement over prob. dist. of events "matters" only insofar as it affects prob. dist. over outcomes; to 3) the dependence payoff; 4) conflict will matter for some actions, not for others; 5) one conflict will affect one pair of actions "a lot" rather than only a "little" (or not at all); other conflicts - other pairs.

b.g.	A	B	C	D
I	a	a	b	b
II	b	b	c	c

Conflict of own prob. but may cooperation
 $(1,0,0,0)$ to $(0,0,0,1)$.

at the only "obliging" position that intervene is:

$$\text{for } (A \vee B) \stackrel{?}{\geq} \text{for } (C \vee D)$$

If there is action similar to I - which

	A	B	C	D
I'	$a+\epsilon$	\bar{a}	b	b
I''	0	$\bar{a}+\epsilon$	b	b

where ϵ is small relative to $(a-b)$.

There may be "secondly" interest in position: for $A \stackrel{?}{\geq} \text{for } B$

The "difference it ^{may} makes" which prob. dist. is selected out of to improve intelligence info is measured by : 2) Minimum difference between the expected values of actions in the indeterminate "conflict set" as prob. dist. ranges over possible set; perhaps, minimum maximum dist., looking at differences between all pairs of actions for each dist.

(a) Maximum maximum dist.

In example above, (a) is $(\delta - \delta)$ (for prob. dists $(1, 1-\lambda, 0, 0)$ and $(0, 0, \lambda, 1-\lambda)$).

(b) is ~ 0 , for prob. dists in which $(P_1 + P_2) - (P_3 + P_4) \rightarrow 0$

(c) "Average difference" corresponding to prob. dist. chosen "at random" among dists in conflict. (To compute, have to compute differences for all dists >).

(d) may be taken as the "value" of the info: $p_{\text{II}}(A \cup B) > p_{\text{II}}(C \cup D)$; if otherwise II had been taken, the difference in expected value for some members of committee would ~~range from~~ be $(\delta - \delta)$.

Committee role: investigate voting procedures, where members disagree on ordering of actions.

Agreement, or good reason, on distribution will necessary; within that, over events or over diets & over outcomes need be urgently determined to determine choice of action. (This, Grublock can often be broken by inventing new action which is agreed by all to be optimal — not necessarily dominant — despite disagreement over diets. Dominant action is reported only when (a) disagreement over diets covers whole range of possible diets, or (b) analyst is ignorant about or makes no assumptions about range of conflict over diets.)

Similarly analysis is worth to look for dominant action; look for optimal action w.r.t. to specific range of diets considered. (contrary to what Wolfe believes).

Potential value of intelligence depends on possible difference in expected value of action that might be chosen after receipt of possible intell., and the expected value of the action^X that would have been chosen without more info; both of these depend on committee's decision rule.

Compute this value for "amount of intell. that could change committee choice from X to (Y, Z, \dots) "; and for intell. that could change it to $(Y, Z, \dots; A, B, \dots)$. Then estimate prob. that a given act of intelligence gathering would generate "this much" info.

i.e. roughly classify "lots of intelligence" in terms of ability to change committee action from ~~another~~ to another the action that would otherwise result from committee decision rule to ~~some other~~ given sets of other actions. Then compute Value of intelligence of a given lot.

Forget & 25 3 Risks involved in evaluating quality of an individual's judgment especially subject to ignorance. Result of applying Ellsberg rule conservatively is that it is hard to get anyone to gamble large sums in supplying an individual with money (many individuals are really "good bets" — but which ones?).

Get more a man with good judgment needs large sums, large scope of decisions, to avoid effects of "bad luck". To get it: a) personal fortunes help, b) partnership allows two men who trust themselves and each other to pool their own capital and individual sources of credit; c) when big money is involved, can't find enough partners one trusts enough to script full liability for their decisions; so limited liability corporation is formed.

(Is there any disadvantage, to investor or creditor, in corp. relative to partnership?)

(Is there more safety, safety, from point of view of backer, in the decision-making processes of a committee, or corp., than individual?

On the other hand, big money may come only to good, bold individuals — not committee — so premium on inside knowledge + study of management).

"Consolidation of risks" is necessary both with "objective" risks and "subjective".
Difference (which Answer questions) is that the reduction of risk achieved is
"objective" + "measurable" in the first case, much less so in the second; so
problems of getting conservative bases for latter consolidation.

Speculator in "non-objective risks" trusts his own judgment; "objectively" (in eyes of observer) he is reducing risks somewhat by his consolidation of costs (assuming considerable randomness in events, likelihood of strong negative correlation in his bad judgment with true probs) but perhaps not a lot, to be taken.
(Unlike life insurance company).

For risky large sum, person will want to know: "How often
will I have the opportunity to make gambles of this size?"

Specialization of risk-bearing also takes place when risks are "objective";
but the result of the consolidation is then not risky, but "objective certainty".
Difference is in the sort of specialists who undertake to consolidate (w.r.t trust in
their judgment, attitude to risk-bearing) and in their ability to get capital.

		α			
I		0	0	I	0
II		0	0	II	0
					I
					9
					9

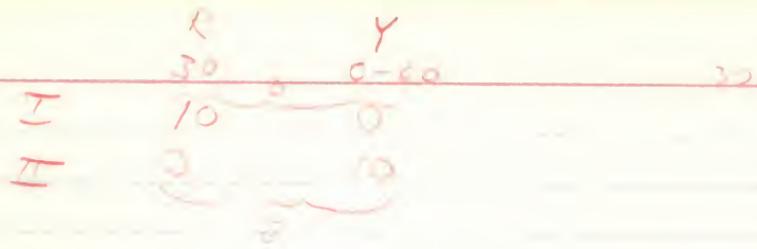
If maxima are equal, no observation less panel cost,
(unbiased?)

minmax right rule is equivalent to minmax rule, and
gives constant outcome (unbiased).

If X is ambiguous, might pay more for observation (if only one of I, II were "available") than if X is any known prob (e.g. $\alpha = \frac{1}{2}$).

i.e. if I 10 0 whereas if $\alpha = \frac{1}{2}$: i.e. II 10 0
 III 3 3 IV 5 5

(By the way: Does Raiffa prefer to flip a coin than to choose I? HA!)



$$b > 0$$

$$\begin{array}{ccccccc}
 & & & 1 & 1 & 1 & \\
 0 & 10 & 0 & -9 & 2 & 1 & 1.1 & 0 \\
 10 & 0 & 0 & 2 & -9 & 1 & 0 & -1.1
 \end{array}$$

$P_1 \cdot 1 > 1 \cdot P_2$
 $P_1 > 10P_2$
 $P_2 >$

$$\begin{array}{ccc}
 6 & 6 & -104 \\
 0 & 10 & -100
 \end{array}$$

$6P_1 > 4P_2 + 4P_3$

$$\begin{array}{ccccc}
 0 & 1 & 0 & 0 & 4 & 4 \\
 1 & 0 & 0 & 6 & 0 & 0
 \end{array}$$

$$P_1 > \frac{2}{3}(P_2 + P_3)$$

$$\begin{array}{ccc}
 4 & 1 & -2 \\
 4 & -2 & -1 \\
 3 & 0 & 0
 \end{array}$$

$$\begin{array}{ccc}
 1 & 1 & 1 \\
 1 & 1 & 1 \\
 1 & 1 & 1
 \end{array}$$

$$P_1 \geq \frac{1}{2}(P_2 + P_3) =$$

$$P_3 \geq 1.5(P_1 + P_2)$$

$$2P_1 = P_2 \cdot 1 + P_3 \cdot 1$$

$$\begin{array}{cc|cc}
 1 & 1 & 1 & 1 \\
 -1 & 2 & 2 & 3 \\
 2 & -1 & 2 & 0 \\
 2 & 2 & -1 & 0 \\
 .5 & .5 & 2 & 1.5 \\
 \hline
 1 & 1 & 1 & 0
 \end{array}$$

	5	5	-105 -105	5	5	5
I	0	10	-100	10	0	0
II	10	0	-100	0	10	0
III	9	9	-102	1	1	1
IV	-2	-2	-108			
			-30			
			-30			
			= 33 27 $\frac{1}{3}$			

$$P_1 \cdot 5 > P_2 \cdot 5 + P_3 \cdot 5 \Leftrightarrow P_1 > 5(P_2 + P_3)$$

$$P_2 > P_1$$

$$P_1 \cdot 10 = P_2 \quad P_1 \cdot 10 > \underline{P_2 \cdot 1 + P_3 \cdot 1} =$$

Condition for III to be preferable to I: $\overset{9}{\text{Inferior to}}$ II:

$$P_1 > \frac{1}{9}(P_2 + P_3) \qquad P_2 > \frac{1}{9}(P_1 + P_3)$$

Condition for IV to be preferable to II:

$$P_1 \cdot 2 > P_2 \cdot 8 + P_3 \cdot 8 \Leftrightarrow P_1 > 8(P_2 + P_3)$$

$$\text{Rule like } P_{\text{out}} = 1-p [\alpha Y_{\max} + (1-\alpha) Y_{\min}]$$

implies: apply several decision criteria; if they conflict,
weight their results as desired.

["Which has higher max? Higher min? Higher average?
Higher ~~average~~ ^{max}? Higher estimated expectation?

Hyp: Max Minimax regret action is preferable if uncertainty is great
enough (i.e. if ^{or} every P_i , $i=1 \dots n$, $P_i > \frac{1}{k}$, $k > n$.